

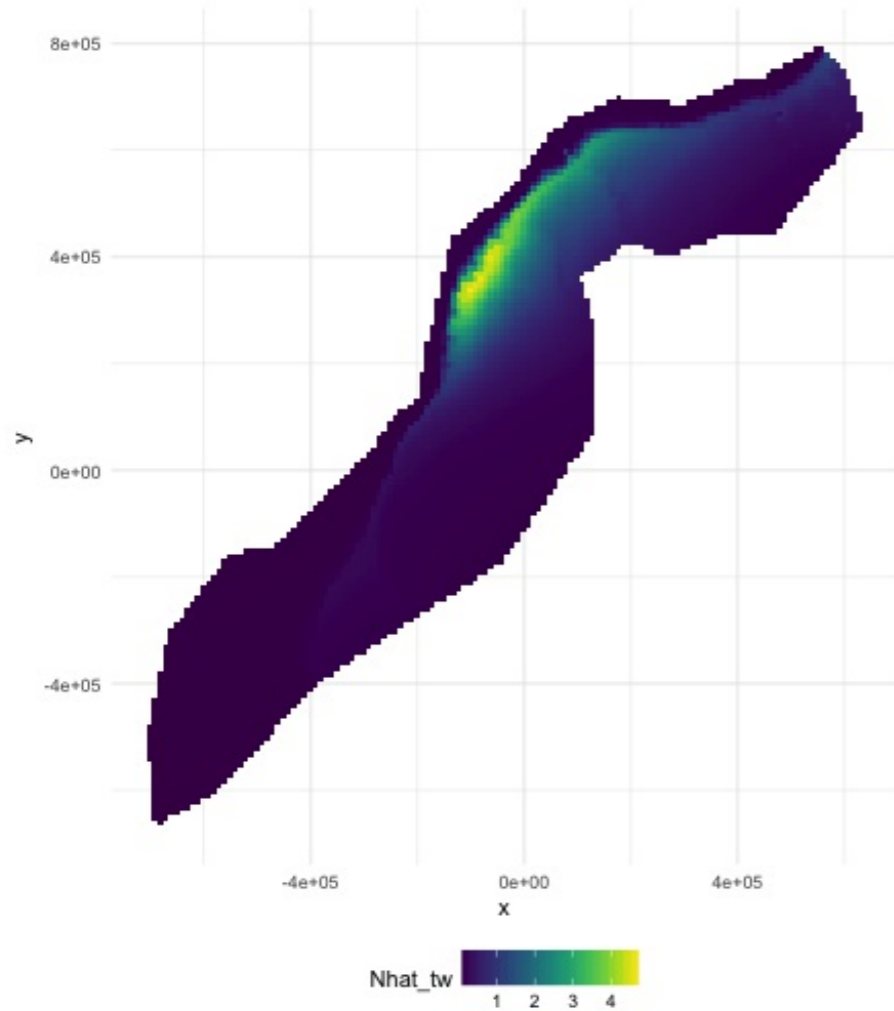
Making predictions

So far...

- Build, check & select models for detectability
- Build, check & select models for abundance
- Make some ecological inference about smooths
- **What about predictions?**

Let's talk about maps

What does a map mean?



- Grids!
- Cells are abundance estimate
- “snapshot”
- Sum cells to get abundance
- Sum a subset?

Going back to the formula

(Count) Model:

$$n_j = A_j \hat{p}_j \exp[\beta_0 + s(y_j) + s(\text{Depth}_j)] + \epsilon_j$$

Predictions (index r):

$$n_r = A_r \exp[\beta_0 + s(y_r) + s(\text{Depth}_r)]$$

Need to “fill-in” values for A_r , y_r and Depth_r .

Predicting

- With these values can use predict in R
- `predict(model, newdata=data)`

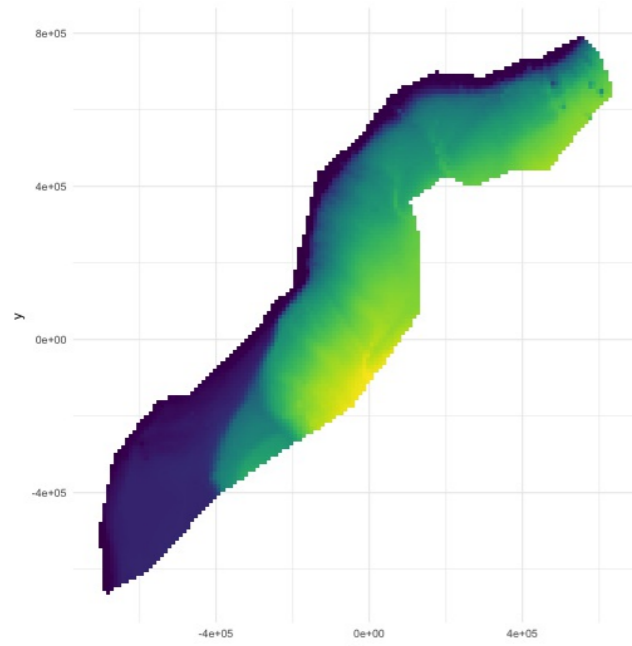
Prediction data

	x	y	Depth	SST	NPP	DistToCAS	EKE	off.set	
	126	547984.6	788254	153.5983	8.8812	1462.521	11788.974	0.0074	1e+08
	127	557984.6	788254	552.3107	9.2078	1465.410	5697.248	0.0144	1e+08
	258	527984.6	778254	96.8199	9.6341	1429.432	13722.626	0.0024	1e+08
	259	537984.6	778254	138.2376	9.6650	1424.862	9720.671	0.0027	1e+08
	260	547984.6	778254	505.1439	9.7905	1379.351	8018.690	0.0101	1e+08
	261	557984.6	778254	1317.5952	9.9523	1348.544	3775.462	0.0193	1e+08
	LinkID	Nhat_tw							
	126	1	0.01417657						
	127	2	0.05123483						
	258	3	0.01118858						
	259	4	0.01277096						
	260	5	0.04180434						
	261	6	0.45935801						

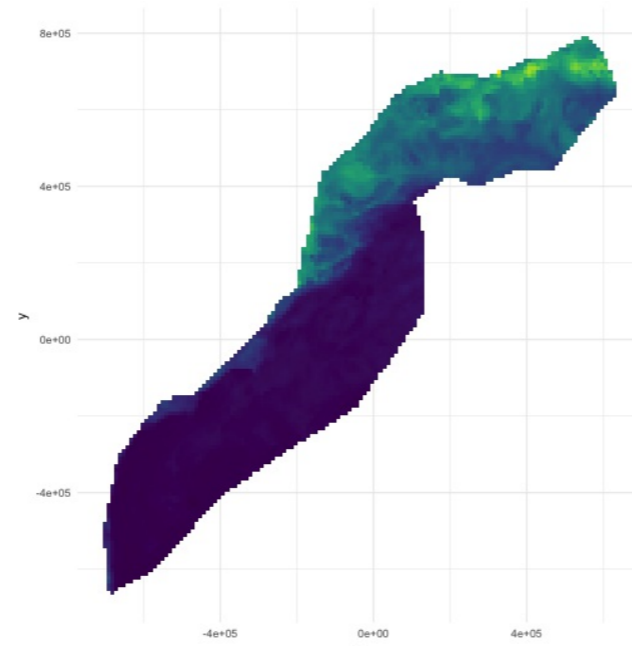
A quick word about rasters

- We have talked about rasters a bit
- In R, the `data.frame` is king
- Fortunately `as.data.frame` exists
- Make our “stack” and then convert to `data.frame`

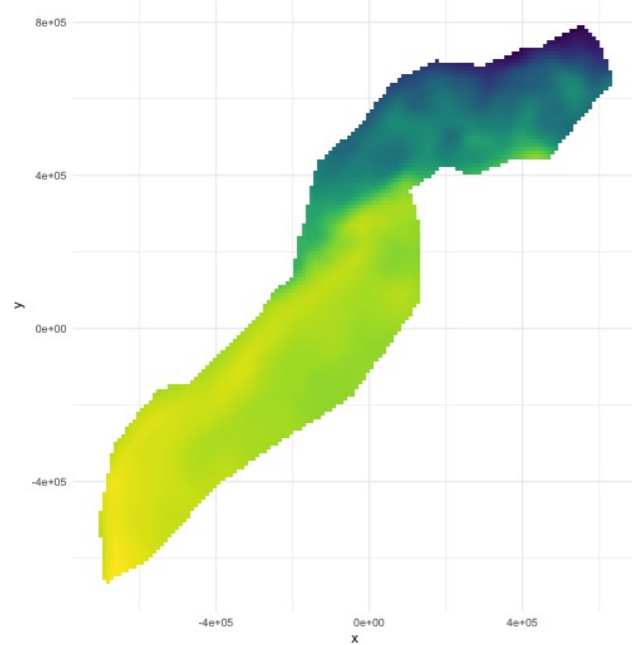
Predictors



Depth
1000000000000000000



NPP
500 1000 1500 2000



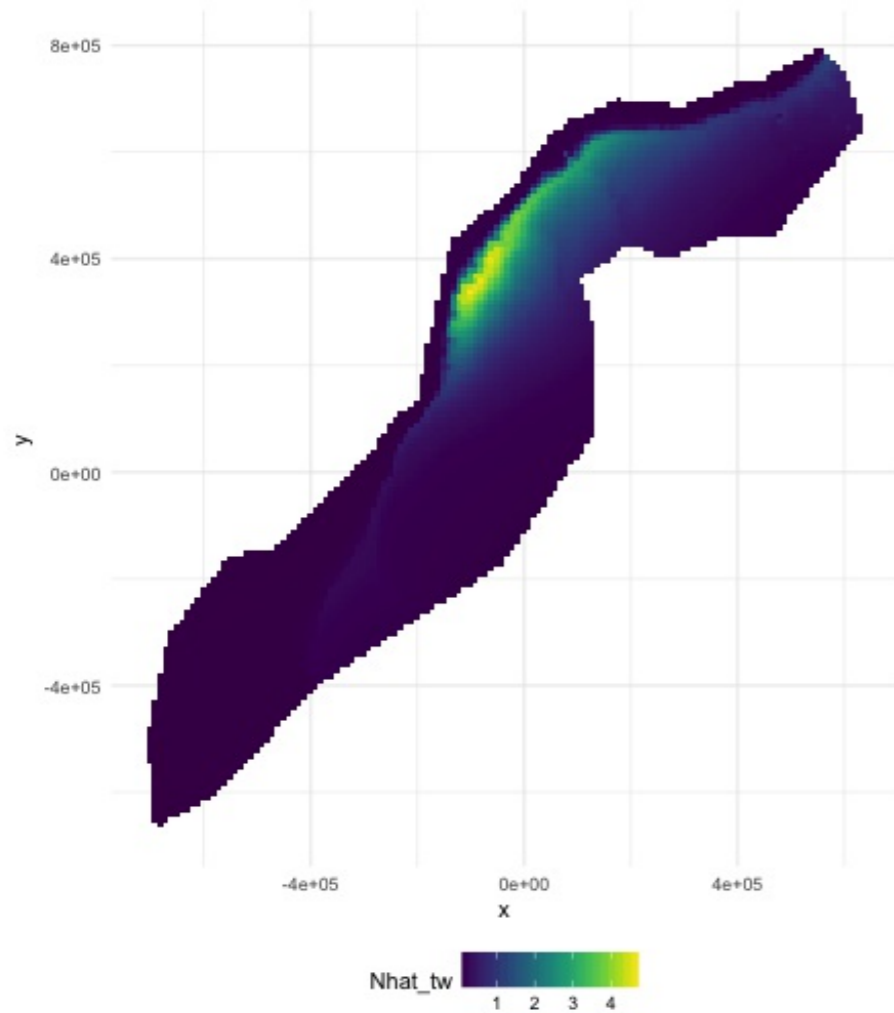
SST
10 15 20 25

Making a prediction

- Add another column to the prediction data
- Plotting then easier (in R)

```
predgrid$Nhat_tw <- predict(dsm_all_tw_rm, predgrid)
```

Maps of predictions



```
p <- ggplot(predgrid) +  
  geom_tile(aes(x=x, y=y,  
               fill=Nhat_tw)) +  
  scale_fill_viridis() +  
  coord_equal()  
print(p)
```

Total abundance

Each cell has an abundance, sum to get total

```
sum(predict(dsm_all_tw_rm, predgrid))
```

```
[1] 2491.864
```

Subsetting

R subsetting lets you calculate “interesting” estimates:

```
# how many sperm whales at depths less than 2500m?  
sum(predgrid$Nhat_tw[predgrid$Depth < 2500])
```

```
[1] 1006.272
```

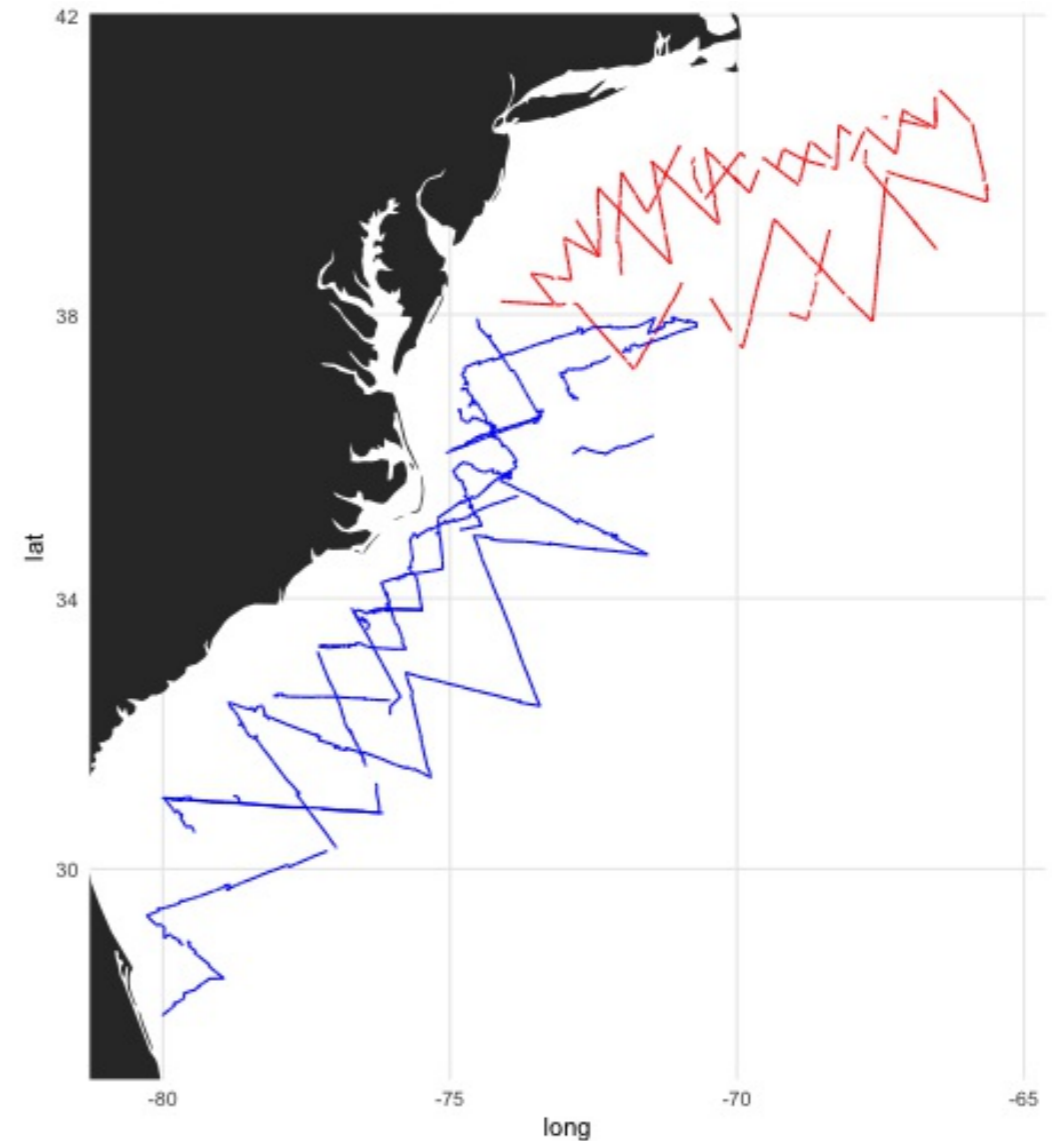
```
# how many sperm whales North of 0?  
sum(predgrid$Nhat_tw[predgrid$x>0])
```

```
[1] 1383.742
```

Extrapolation

What do we mean by extrapolation?

- Predicting at values outside those observed
- What does “outside” mean?
 - between transects?
 - outside “survey area”?

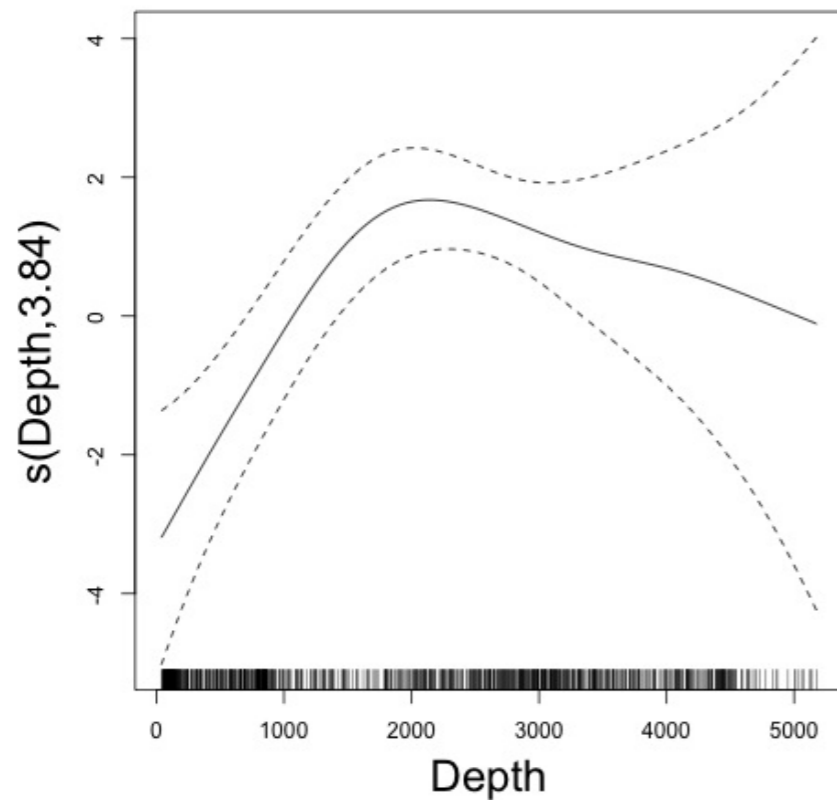


Temporal extrapolation

- Models are temporally implicit (mostly)
- Dynamic variables change seasonally
- Migration can be an issue
- Need to understand what the predictions **are**

Extrapolation

- Extrapolation is fraught with issues
- Want to be predicting “inside the rug”
- In general, try not to do it!
- (Think about variance too!)



Recap

- Using predict
- Getting “overall” abundance
- Subsetting
- Plotting in R
- Extrapolation (and its dangers)

Estimating variance

Now we can make predictions

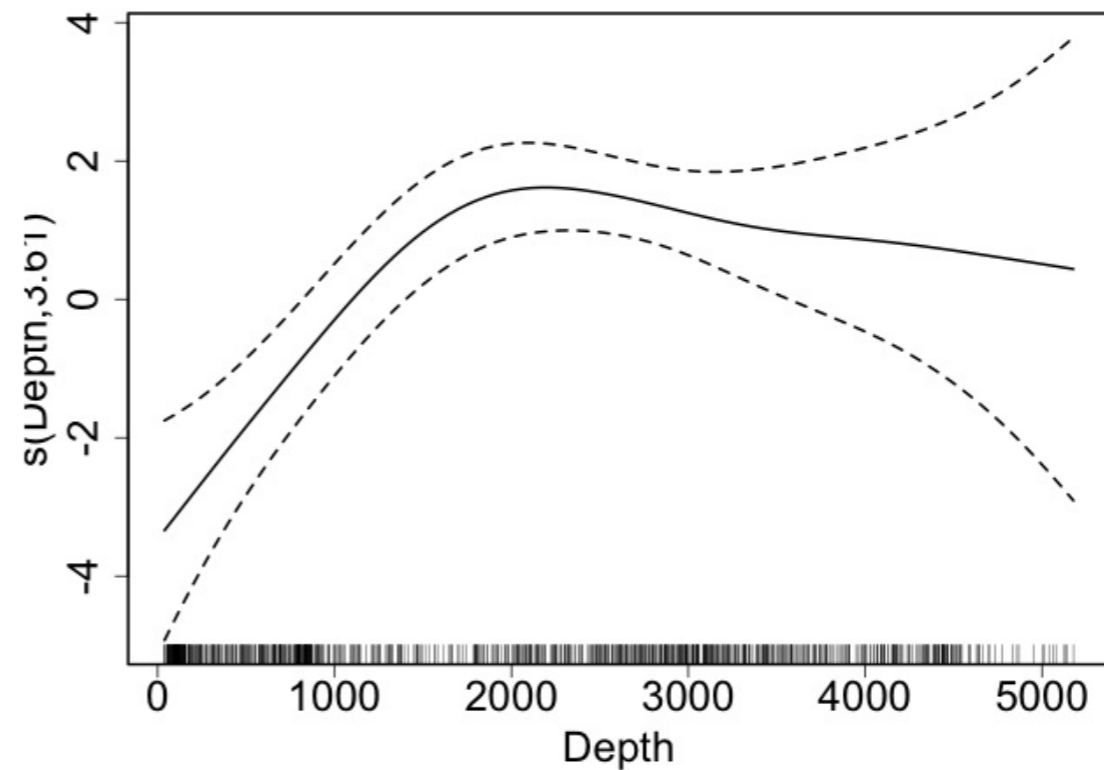
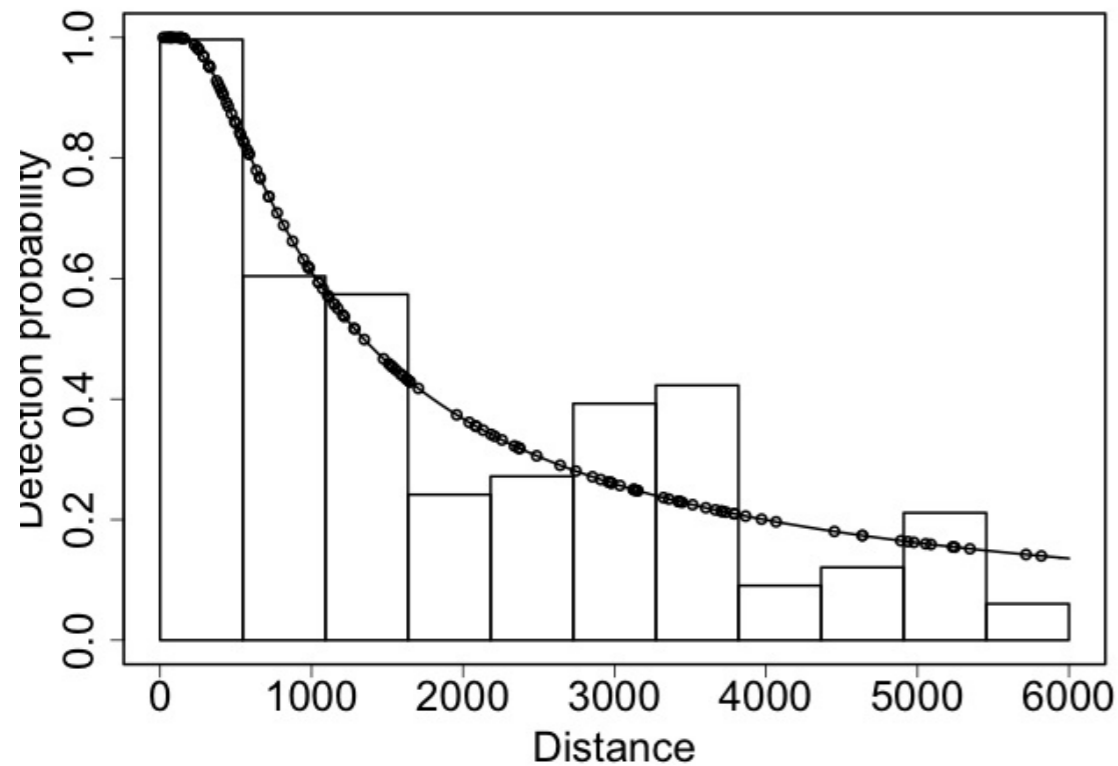
Now we are dangerous.

Predictions are useless
without uncertainty

Where does uncertainty come from?

Sources of uncertainty

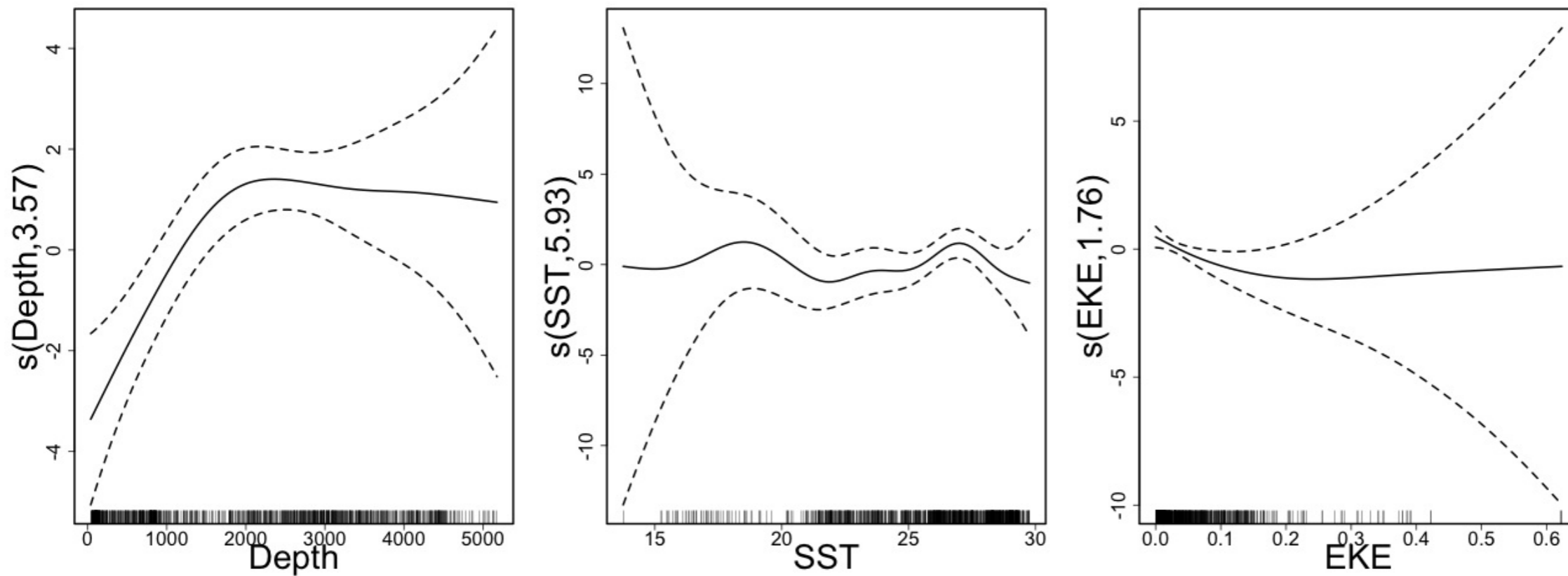
- Detection function
- GAM parameters



Let's think about smooths first

Uncertainty in smooths

- Dashed lines are +/- 2 standard errors
- How do we translate to \hat{N} ?



Back to bases

- Before we expressed smooths as:

- $s(x) = \sum_{k=1}^K \beta_k b_k(x)$

- Theory tells us that:

- $\boldsymbol{\beta} \sim N(\hat{\boldsymbol{\beta}}, \mathbf{V}_\beta)$

- where \mathbf{V}_β is a bit complicated

- (derived from the smoother matrix)

Predictions to prediction variance (roughly)

- “map” data onto fitted values $\mathbf{X}\boldsymbol{\beta}$
- “map” prediction matrix to predictions $\mathbf{X}_p\boldsymbol{\beta}$
- Here \mathbf{X}_p need to take smooths into account
- pre-/post-multiply by \mathbf{X}_p to “transform variance”
 - $\Rightarrow \mathbf{X}_p^T \mathbf{V} \boldsymbol{\beta} \mathbf{X}_p$
 - link scale, need to do another transform for response

Adding in detection functions

GAM + detection function uncertainty

(Getting a little fast-and-loose with the mathematics)

$$\text{CV}^2 (\hat{N}) \approx \text{CV}^2 (\text{GAM}) + \text{CV}^2 (\text{detection function})$$

Not that simple...

- Assumes detection function and GAM are **independent**
- **Maybe** this is okay?
- (Probably not true?)

Variance propagation

- Include the detectability as term in GAM
- Random effect, mean zero, variance of detection function
- Uncertainty “propagated” through the model
- Details in bibliography (too much to detail here)
- Under development
- (Can cover in special topic)

That seemed complicated...

R to the rescue

In R...

- Functions in dsm to do this
- `dsm.var.gam`
 - assumes spatial model and detection function are independent
- `dsm.var.prop`
 - propagates uncertainty from detection function to spatial model
 - only works for count models (more or less)

Variance of abundance

Using dsm.var.gam

```
dsm_tw_var_ind <- dsm.var.gam(dsm_all_tw_rm, predgrid,  
                             off.set=predgrid$off.set)  
summary(dsm_tw_var_ind)
```

Summary of uncertainty in a density surface model calculated
analytically for GAM, with delta method

Approximate asymptotic confidence interval:

2.5% Mean 97.5%
1539.018 2491.864 4034.643

(Using log-Normal approximation)

Point estimate : 2491.864
CV of detection function : 0.2113123
CV from GAM : 0.1329
Total standard error : 622.0389
Total coefficient of variation : 0.2496

Variance of abundance

Using dsm.var.prop

```
dsm_tw_var <- dsm.var.prop(dsm_all_tw_rm, predgrid,  
                          off.set=predgrid$off.set)  
summary(dsm_tw_var)
```

Summary of uncertainty in a density surface model calculated
by variance propagation.

Probability of detection in fitted model and variance model

	Fitted.model	Fitted.model.se	Refitted.model
1	0.3624567	0.07659373	0.3624567

Approximate asymptotic confidence interval:

	2.5%	Mean	97.5%
	1556.898	2458.634	3882.646

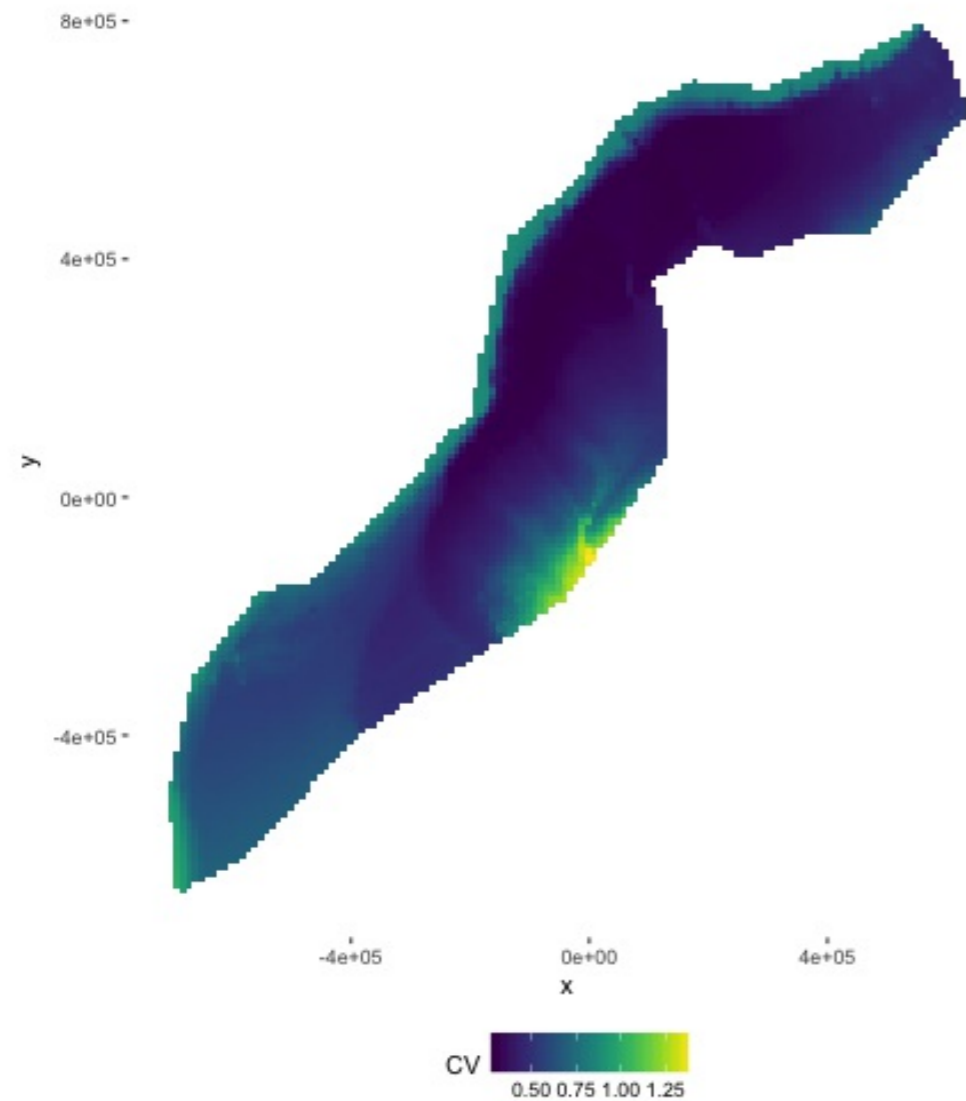
(Using log-Normal approximation)

Point estimate	: 2458.634
Standard error	: 581.0379
Coefficient of variation	: 0.2363

Plotting - data processing

- Calculate uncertainty per-cell
- `dsm.var.*` thinks predgrid is one “region”
- Need to split data into cells (using `split()`)
- (Could be arbitrary sets of cells, see exercises)
- Need width and height of cells for plotting

CV plot

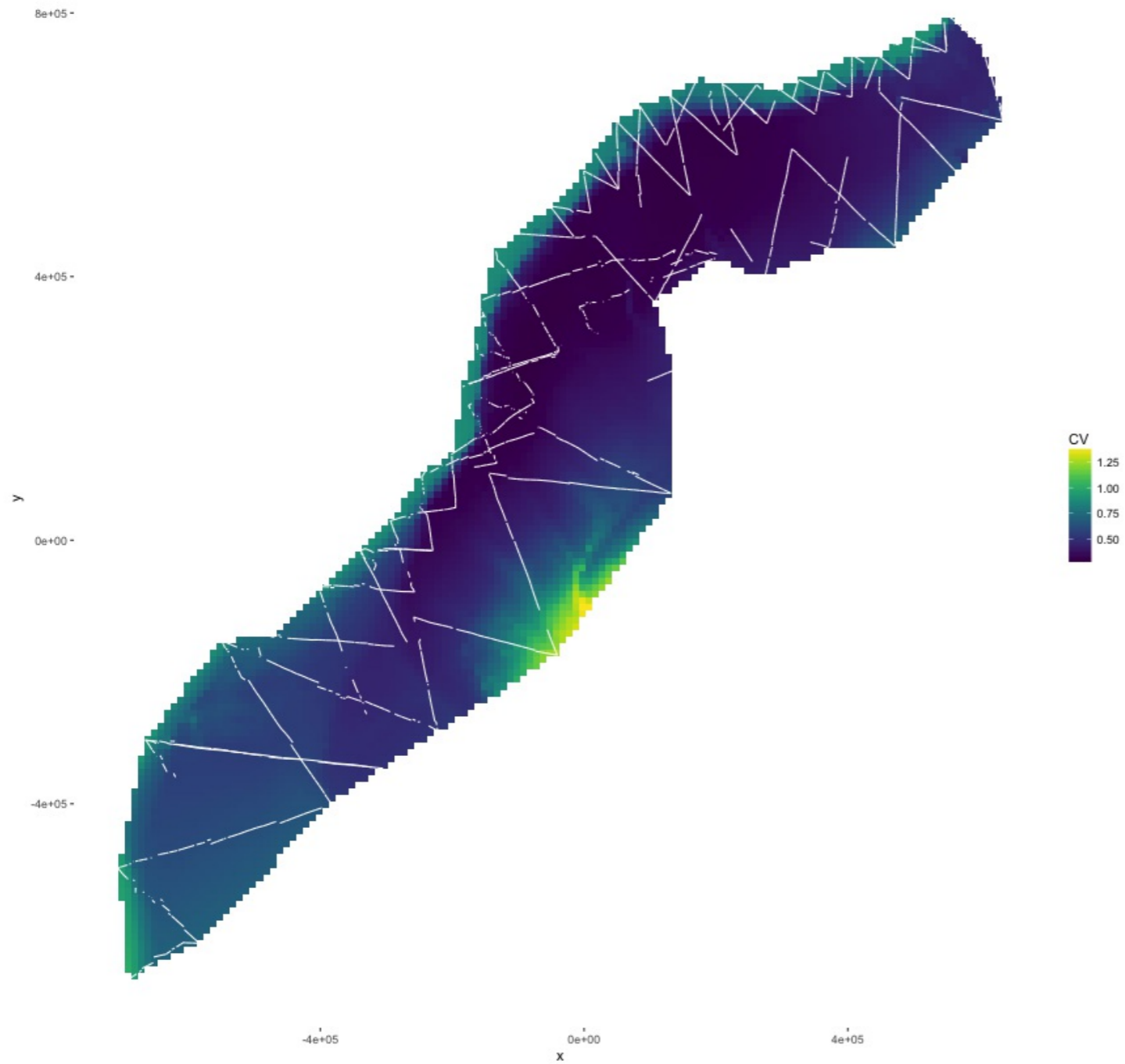


```
p <- plot(dsm_tw_var_map,  
observations=FALSE, plot=FALSE) +  
  coord_equal() +  
  scale_fill_viridis()  
print(p)
```

Interpreting CV plots

- Plotting coefficient of variation
- Standardise standard deviation by mean
- $CV = se(\hat{N}) / \hat{N}$ (per cell)
- Can be useful to overplot survey effort

Effort overplotted



Big CVs

- Here CVs are “well behaved”
- Not always the case (huge CVs possible)
- These can be a pain to plot
- Use `cut()` in R to make categorical variable
 - e.g. `c(seq(0,1, len=100), 2:4, Inf)` or `somesuch`

Recap

- How does uncertainty arise in a DSM?
- Estimate variance of abundance estimate
- Map coefficient of variation

Let's try that!